cylindrical space.

Deep Generative for High Energy F

			I		
	-	Convolution		Max-Pool	
Jet Im	age				

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UCSD PHYS 139/239 March 7, 2023

Introduction: generative models

A **generator** is nothing other than a function that maps random numbers to structure.

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Deep generative models: the map is a deep neural network.



GANs

Generative Adversarial Networks

Restricted Botlzmann Machines

Scorebased

Mixture Density Networks

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NFS Normalizing Flows

Energybased models

VAEs

Variational Autoencoders

Tools - focus for today

GANs

Generative Adversarial Networks

Restricted Botlzmann Machines Scorebased Mixture Density Networks

VAEs

Variational Autoencoders

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NFS Normalizing Flows

Energybased models

Outline

- 1. Why Generative Models?
- 2. Warm up: mixture density networks
- 3. Next: brief overview of GANs, VAEs, NFs
- 4. Statistical amplification
- 5. Applications
- 6. Bonus



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Why generative models?

1. Augment/replace slow physics-based simulations

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- 2. (Fast) Confidence Intervals / Posterior Analysis
- 3. Background estimation / anomaly detection





If you know the family of functions that generated your data, you can't beat fitting that function.

(I'll be more precise later about "beat")

A lot of physics data are nearly Gaussian, or combinations of a small number of Gaussians, possibly with a complex dependence on energy, time, etc.

Classical mixture model:

$$p(x) \propto \sum_{i} \alpha_{i} \exp\left(-\frac{1}{2}(x-\mu)^{T} \Sigma^{-1}(x-\mu)\right)$$



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$$p(x) \propto \sum_{i} \alpha_{i} \exp\left(-\frac{1}{2}(x-\mu)^{T}\Sigma^{-1}(x-\mu)\right)$$

 $\begin{array}{l} \text{Mixture density network:} \\ p(x \,|\, z) \propto \sum_i \alpha_i(z) \, \exp\left(-\frac{1}{2}(x-\mu(z))^T \Sigma(z)^{-1}(x-\mu(z))\right) \end{array} \end{array}$

Mixture density network:

$$p(x | z) \propto \sum_{i} \alpha_{i}(z) \exp\left(-\frac{1}{2}(x - \mu(z))^{T}\Sigma(z)^{-1}(x - \mu(z))\right)$$

The "parameters" $\alpha(z), \mu(z), \Sigma(z)$ are deep neural networks.

Since Σ is symmetric and positive semi-definite, need to take care when designing its architecture.

Train an MDN by minimizing $-\log(p(x | z))$.

When x is 1D, there is only one component, and Σ is fixed, then this reduces to mean squared error!

MDNs: code

from tensorflow import keras
import tensorflow probability as tfp

steps per epoch=n // batch size)

```
tfd = tfp.distributions
tfpl = tfp.layers
tfk = tf.keras
tfkl = tf.keras.layers
n = len(X[:,0:])
z = np.zeros(n)
x = X[:, 0:]
# Model the distribution of y given x with a Mixture Density Network.
event shape = np.shape(X)
num components = 5
params size =
tfpl.MixtureSameFamily.params size(num components, component params size=tfpl.MultivariateNormalTriL.params size(event shape[0]))
model = tfk.Sequential([
  tfkl.Dense(32, activation='relu'),
  tfkl.Dense(64, activation='relu'),
  tfkl.Dense(64, activation='relu'),
  tfkl.Dense(params size, activation=None),
  tfpl.MixtureSameFamily(num_components, tfpl.MultivariateNormalTriL(event_shape[0]))
])
# Fit.
batch size = 100
model.compile(optimizer='adam',
              loss=lambda x, model: -model.log prob(x))
myhistory = model.fit(z, x,
          batch size=batch size,
          epochs=50,
```

(equivalently simple in PyTorch)

MDNs in action



Simultaneously learn confidence interval ("resolution") and point estimate

Example: energy regression for hadrons in the ATLAS calorimeter

(figures without citations are links)



MDNs: overview

Pros:

- Access to the density
- Fast to sample
- Easy to specify
- Easy to train

Cons:

- Do not scale well to high dimensions
- Not good when the data are not nearly Gaussian(s)

Up next: deep generative models with more flexibility



GANs

Generative Adversarial Networks

Restricted Botlzmann Machines Scorebased Mixture Density Networks

VAEs

Variational Autoencoders

15

NFS Normalizing Flows

Energybased models

Generative Adversarial Networks (GANs): *A two-network game where one maps noise to structure and one classifies images as fake or real.*

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Vanilla GAN loss: $-\sum_{X\sim data} \log(D(x)) - \sum_{Z\sim noise} \log(1 - D(G(z)))$

There are many variations on this theme*.

One important variation is called the Wasserstein or WGAN.

Schematically, the idea of WGAN is to replace the discriminator with a notion of distance ('earth moving') between the real and fake data

*see e.g. https://github.com/hindupuravinash/the-gan-zoo



GANs: overview

Pros:

- Fast to sample
- Easy to specify (no restrictions on G)
- Easy to make high dimensional

Cons:

- No access to density
- (Very) Hard to train (minimax)
- Mode collapse

Introduction: AEs

Autoencoders (AEs):

A pair of networks that embed the data into a latent space and decode back to the data space.



Physics-based simulator or data

encoder

decoder

Introduction: VAEs

Variational Autoencoders (VAEs):

A pair of networks that embed the data into a latent space with a given prior and decode back to the data space.



Introduction: VAEs



Why "variational"? Another way of looking at this is the Evidence Lower Bound (ELBO) and p(z|x) is the variational posterior.

VAEs: overview

Pros:

- Fast to sample
- Easy to specify (no restrictions on G)
- Easy to make high dimensional
- Easy to train

Cons:

- No access to density
- Tends to over-smooth the density

ex. AE variations: β -VAE, PAE



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Normalizing Flows (NFs): *A series of invertible transformations mapping a known density into the data density.*

Optimize via maximum likelihood



latent space

p(Z)

Invertible transformations with tractable Jacobians

Loss: $-\log(p(x))$

$$p(x) = p(z) \left| \frac{dF^{-1}}{dx} \right|$$



In case you have not seen the change of variables formula...



Normalizing Flows (NFs): *A series of invertible transformations mapping a known density into the data density.*

Optimize via maximum likelihood



latent space

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Invertible transformations with tractable Jacobians

Loss: $-\log(p(x))$

$$p(x) = p(z) |dF^{-1}/dx$$



Normalizing Flows (NFs): *A series of invertible transformations mapping a known density into the data density.*

Example:
$$F(x_i) = z_i + NN(x_{i-1})$$

("autoregressive")

Optimize via maximum likelihood

28



latent space

p(Z)

Invertible transformations with tractable Jacobians

$$p(x) = p(z) \left| \frac{dF^{-1}}{dx} \right|$$



NFs: overview

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Pros:

- Usually only fast to sample OR to estimate the density
- Access to the density
- Easy to train

Cons:

- Sometimes hard to make expressive enough
- "Generator" is highly limited in form
- Cannot learn topology

Introduction: Score-based

Score-based Learn the gradient of the density instead of the probability density itself.

> "score" Loss: $|f(x) - \nabla p(x)|^2$

...but since we don't know ∇p , we make use of a trick whereby the data are perturbed and it is sufficient to match the score of the perturbing function (!)

This turns the problem into a stochastic differential equation which is the same as diffusion (sometimes this is called a "diffusion model")

Introduction: Score-based

Score-based Learn the gradient of the density instead of the probability density itself.



Score-based: overview

Pros:

- Many of the benefits of a NF, but unrestricted functions
- Access to the density with some work
- Easy to train
- Currently the "best" on the market

Cons:

• A bit slow to train / evaluate

Image Generation on CIFAR-10

Rank	Model	FID & FID- 10k	Inception score	bits/dimension	10k- test	Paper	Code	Result	Year	Tags 🗷
1	EDM-G++ (unconditional)	1.77		2.55		Refining Generative Process with Discriminator Guidance in Score-based Diffusion Models	0	Ð	2022	Diffusion Score-based
2	StyleGAN-XL	1.85				StyleGAN-XL: Scaling StyleGAN to Large Diverse Datasets	o	Ð	2022	GAN
3	STF (unconditional)	1.90				Stable Target Field for Reduced Variance Score Estimation in Diffusion Models	0	Ð	2023	Score-based
4	LSGM-G++ (FID)	1.94		3.42		Refining Generative Process with Discriminator Guidance in Score-based Diffusion Models	0	Ð	2022	Score-based
5	PSLD (ODE)	2.10	9.93			Generative Diffusions in Augmented Spaces: A Complete Recipe	0	Ð	2023	Score-based
6	LSGM (FID)	2.10		3.43		Score-based Generative Modeling in Latent Space	0	÷	2021	Score-based VAE
7	Subspace Diffusion (NSCN++)	2.17	9.99			Subspace Diffusion Generative Models	0	Ð	2022	Score-based
8	LSGM (balanced)	2.17		2.95		Score-based Generative Modeling in Latent Space	0	Ð	2021	VAE Score-based
9	NCSN++	2.20	9.73			Score-Based Generative Modeling through Stochastic Differential Equations	0	Ð	2020	Score-based
10	PSLD (SDE)	2.21				Generative Diffusions in Augmented Spaces: A Complete Recipe	0	Ð	2023	Score-based

A few words about statistics



Statistical Amplification

Performance continues to improve on many fronts. As we integrate these tools into our workflows, we need to think about uncertainties.

One question is about the **statistical power** of samples from a generative model. This depends on the implicit or explicit information we encode in the networks.



See also 1909.03081, 2002.06307, 2104.04543 (Generative Bayesian NNs), and 2107.08979 ("resampling")

Impact of (re)parameterize

4000

Generative models are NOT investor and the states wises yield transformations. Choose your coordinates wises yield to 12.5








M. Mustafa, et al., Comp. Astrophysics and Cosmology 6 (2019)



M. Paganini, L. De Oliveira, B. Nachman, Phys. Rev. Lett. 120 (2018) 042003

view Background estimation

N. Krachmalnicoff and G. Puglisi, arXiv:2011.02221

The Structur Infer Parton/particle-Radiation in the Quantum Strong Ford Evel Dynamics Synthetic Universes for Dark Matter Parton/particlelevel simulations

deg



Y. S. Lai, D. Neill, M. Płoskoń, F. Ringer, arXiv:2012.06582

M. Mustafa, et al., Comp. Astrophysics and Cosmology 6 (2019)

Accelerating Detector Simulations



Calorimeters are often the slowest to simulate

40

stopping particles requires simulating interactions of all energies

Grayscale images: Pixel intensity = energy deposited



Calorimeter ML Surrogate Models



Many papers on this subject see the living review for all

47





See also https

3000

Introducing CaloGAN



1705.02355

42

1705.02355

43

Performance: average images

Geant4







A key challenge in training GANs is the diversity of generated images. This does not seem to be a problem for CaloGAN.



Performance: energy per layer



1705.02355

45

Conditioning

Fix noise, scan latent variable corresponding to energy

1711.08813

46



Fix noise, scan latent variable corresponding to x-position



Conditioning

Fix noise, scan latent variable corresponding to energy

1711.08813



1705.02355

Timing



Generation Method	Hardware	Batch Size	milliseconds/shower
GEANT4	CPU	N/A	1772 -
Calogan	CPU Intel Xeon E5-2670	1	13.1
		10	5.11
		128	2.19
		1024	2.03
		1	14.5
		4	3.68
	GPU	128	0.021
	NVIDIA K80	512	0.014
		1024	0.012 -

(clearly these numbers have changed as both technologies have improved - this is simply meant to be qualitative & motivating!)

Generative models have gotten much better; flow models are particularly promising. Added bonus: have an explicit density.



2106.05285

49

2106.05285

50

Current State of the art

Generative models have dotten much better:

AUC / JSD		DNN		
		vs. CaloGAN	vs. CaloFlow	
°+	unnormalized	1.000(0) / 0.993(1)	$0.847(8) \ / \ 0.345(12)$	
E	normalized	1.000(0) / 0.997(0)	$0.869(2) \ / \ 0.376(4)$	
	unnormalized	$1.000(0) \ / \ 0.996(1)$	$0.660(6) \ / \ 0.067(4)$	
γ	normalized	1.000(0) / 0.994(1)	$0.794(4) \ / \ 0.213(7)$	
π^+	unnormalized	1.000(0) / 0.988(1)	0.632(2) / $0.048(1)$	
Λ	normalized	1.000(0) / 0.997(0)	0.751(4) / 0.148(4)	

Output is nearly indistinguishable from Geant4 !

AUC = 1 means easily distinguishable, AUC = 0.5means not distinguishable

Depth-weighted total energy I_d

Shower Depth Width σ_{s_d}

Shower Depth *s*_d

 π^+ GEANT

 π^+ CaloGAN

 π^+ CaloFlow

How to compare generative models? See e.g. 2211.10295

See also score-based: 2206.11898

2109.02551

51

Integration into real detector sim.



The ATLAS Collaboration fast simulation (AF3) now includes a GAN at intermediate energies for pions

Integration into real detector sim.



The GAN architecture is relatively simple, but it is able to match the energy scale and resolution well.

There is one GAN per η slice



2109.02551

53

Integration into real detector sim.



The new fast simulation (AF3) significantly improves jet substructure with respect to the older one (AF2)

Ideally, the same calibrations derived for full sim. (Geant4-based) can be applied to the fast sim.



2109.02551

54





As expected, the fast sim. timing is independent of energy, while Geant4 requires more time for higher energy.

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Refining Simulations

As we move towards precision, we may need to complement primary generative models with post-hoc correction models (e.g. via reweighting)



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M. Paganini, L. De Oliveira, B. Nachman, Phys. Rev. Lett. 120 (2018) 042003

view Background estimation

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The Structurent of the Action of the Action

Y. S. Lai, D. Neill, M. Płoskoń, F. Ringer, arXiv:2012.06582

Accelerate Slow Parton/particlelevel simulations

Synthetic

0.2 0.4 0.6 0.8 (deg)

Accelerating Parton/Particle Sim.*

Flat jet images with GANs

M. Paganini, L. de Oliveira, B. Nachman

1701.05927

58

Accelerating Parton/Particle Sim.*

Flat jet images with GANs

M. Paganini, L. de Oliveira, B. Nachman



LA = Locally aware; somewhere between a DNN and a CNN

Weight sharing across space





Accelerating Parton/Particle Sim.*



62

Accelerating Parton/Particle Sim.*

Flat jet images with GANs

M. Paganini, L. de Oliveira, B. Nachman 1701.05927 Scale invariant images with AEs J. Monk 1807.03685

Fixed number of 4vectors, allow for intermediate resonances A. Butter, T. Plehn, R. Winterhalder 1907.03764

63

Variable-length output with graphs R. Kansal et al. 2106.11535



M. Paganini, L. De Oliveira, B. Nachman, Phys. Rev. Lett. 120 (2018) 042003

Accelerate Slow

view Background estimation

N. Krachmalnicoff and G. Puglisi, arXiv:2011.02221

The Structurent of the Action of the Action

Parton/particlelevel simulations

Synthetic

Universes for

Dark Matter

M. Mustafa, et al., Comp. Astrophysics and Cosmology 6 (2019)

65

Many cases where simulation is **not good enough** - can train generate models to act as **simulation surrogates**

N.B. everything in I've shown before this, we trained on simulation, not on data (!)

Background Estimation



Many cases where simulation is **not good enough** - can train generate models to act as **simulation surrogates**

Example 1: unbinned templates for QCD jets to extrapolate in jet multiplicity



Background Estimation

Many cases where simulation is **not good enough** - can train generate models to act as **simulation surrogates**

Example 2: unbinned templates for QCD jets to extrapolate in dijet mass





M. Paganini, L. De Oliveira, B. Nachman, Phys. Rev. Lett. 120 (2018) 042003

Synthetic

view Background estimation

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M. Mustafa, et al., Comp. Astrophysics and Cosmology 6 (2019)

Can we use generative models directly for inference? (and not "just" for augmenting/accelerating simulation)

69

70

Infering Parton/particle-level Dynamics

Can we use generative models directly for inference? (and not "just" for augmenting/accelerating simulation)

Example 1: Inferring fragmentation functions



See also 1804.09720 ("JUNIPR") and 2012.06582 (GAN-based)

Infering Parton/particle-level Dynamics



See also 1804.09720 ("JUNIPR") and 2012.06582 (GAN-based)

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Infering Parton/particle-level Dynamics

Can we use generative models directly for inference? (and not "just" for augmenting/accelerating simulation)

Example 2: Unfolding



See also 1911.09107 ("OmniFold") and 2101.08944 ("OTUS")
Bonus: What else can we do?



2112.05722

74

ex. GANs: Symmetry Discovery



The framework of generative models is quite flexible and we can do more than generate events.

> For example, can **discover symmetries** in data!





ex. VAEs: Compression





Automatically vary the compression level by varying β





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ex. NFs: Data Morphing

"Move" instead of "Reweight" with normalizing flows





Outline

- 1. Why Generative Models?
- 2. Warm up: mixture density networks
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Generative models hold great promise for many areas of physics research

This is an area of rapid development at the intersection of theory & experiment and I'm excited for where it will take us!

Examples today were not exhaustive ... Prof. Duarte has also been a pioneer in this area!

This is a link to a recent Berkeley workshop dedicated to generative models →





