

## Policies

Please work on the quiz individually.

## Submission Instructions

Please submit your quiz as a single .pdf file to Gradescope under “Quiz 2”.

## 1 Propagator and Schrödinger Equation [20 Points]

*Relevant materials: Week 2 lectures*

**Problem A [10 points]:** Prove that the free particle propagator

$$\mathcal{K}(x_B, t_B; x_A, t_A) = \left( \frac{m}{2\pi i \hbar (t_B - t_A)} \right)^{1/2} \exp \left[ \frac{im(x_B - x_A)^2}{2\hbar(t_B - t_A)} \right] \quad (1)$$

satisfies the Schrödinger equation

$$-\frac{\hbar}{i} \frac{\partial \mathcal{K}(x_B, t_B; x_A, t_A)}{\partial t_B} = -\frac{\hbar^2}{2m} \frac{\partial^2 \mathcal{K}(x_B, t_B; x_A, t_A)}{\partial x_B^2} \quad (2)$$

by direct substitution.

**Hint:** Without loss of generality, you can set  $x_A = t_A = 0$ .

**Problem B [10 points]:** Using the above, show that any wave function  $\psi(x, t)$  of a free particle also satisfies the Schrödinger equation

$$-\frac{\hbar}{i} \frac{\partial \psi(x, t)}{\partial t} = -\frac{\hbar^2}{2m} \frac{\partial^2 \psi(x, t)}{\partial x^2}. \quad (3)$$

**Hint:** Use the fact that  $\psi(x, t) = \int_{-\infty}^{\infty} \mathcal{K}(x, t; x', t') \psi(x', t') dx'$ .